

# Digital Communication in the Modern World

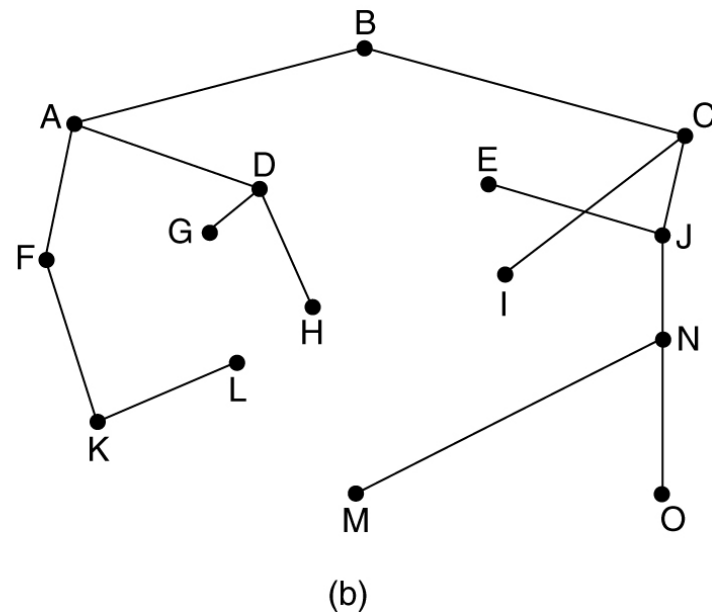
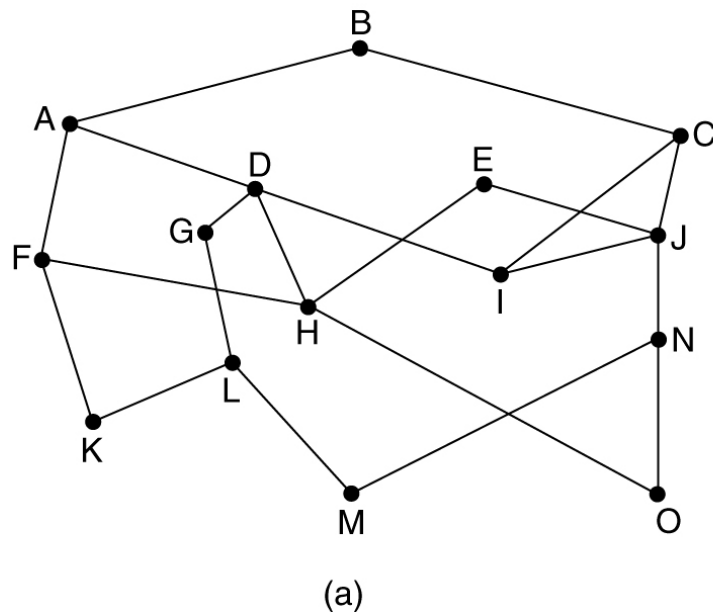
## Network Layer:

### Routing Classifications; Shortest Path Routing

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*Some of the slides have been borrowed from:*  
*Computer Networking: A Top Down Approach Featuring the Internet,*  
*2<sup>nd</sup> edition.*  
Jim Kurose, Keith Ross  
Addison-Wesley, July 2002.

Network Layer's main problem: To get efficiently from one point to the other in a dynamic environment



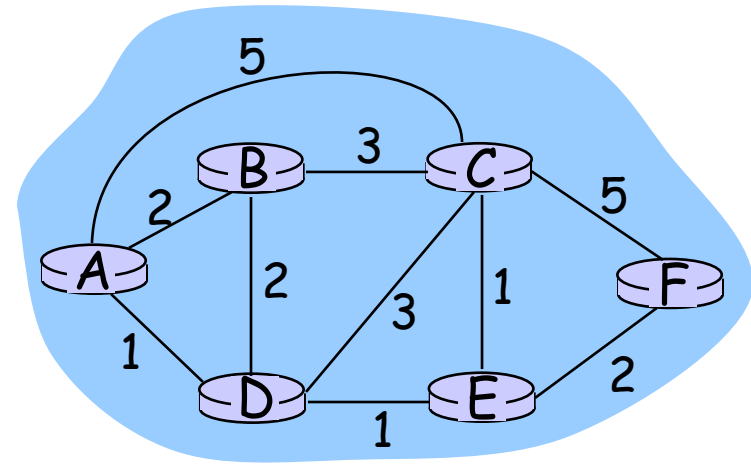
# Routing

## Routing protocol

**Goal:** determine "good" path (sequence of routers) thru network from source to dest.

Graph abstraction for routing algorithms:

- graph nodes are routers
- graph edges are physical links
  - link cost: delay, \$ cost, or congestion level



- "good" path:
  - typically means minimum cost path
  - other def's possible (min. num of links)

# Datagram Routing Algorithm Classification

- Global (Link State) Routing
  - Shortest Path routing
    - Dijkstra routing
- Decentralized
  - Distance Vector routing
- Hierarchical Routing

# A Link-State Routing Algorithm

## Dijkstra's algorithm

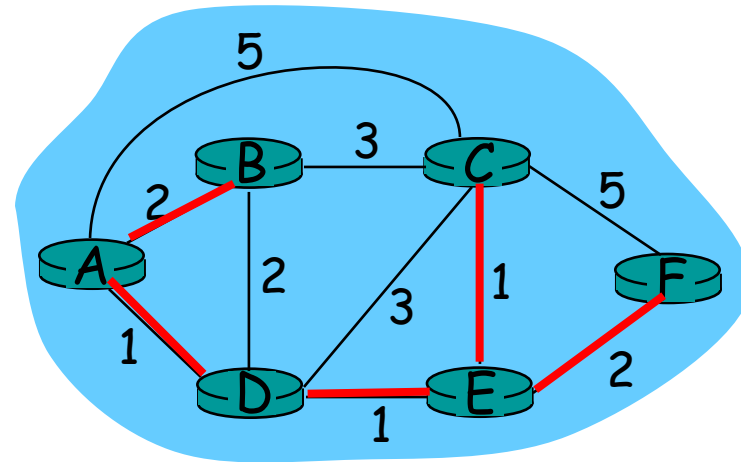
- ❑ net topology, link costs known to all nodes
  - accomplished via "link state broadcast"
  - all nodes have same info
- ❑ computes least cost paths from one node ("source") to all other nodes
  - gives a routing table for that node
- ❑ iterative: after  $k$  iterations, know the *least cost path* to  $k$  dest.'s

## Notation:

- ❑  $c(i,j)$ : link cost from node  $i$  to  $j$ . Cost infinite if not direct neighbors
- ❑  $D(v)$ : current value of cost of path from source to dest.  $V$
- ❑  $p(v)$ : predecessor node along path from source to  $V$ , that is next  $v$
- ❑  $N$ : set of nodes whose least cost path definitively known

# Dijkstra's Algorithm

```
1 Initialization:  
2  $N = \{A\}$   
3 for all nodes  $v$   
4   if  $v$  adjacent to  $A$   
5     then  $D(v) = c(A,v)$   
6     else  $D(v) = \text{infinity}$   
7
```



```
8 Loop  
9   find  $w$  not in  $N$  such that  $D(w)$  is a minimum  
10  add  $w$  to  $N$   
11  update  $D(v)$  for all  $v$  adjacent to  $w$  and not in  $N$ :  
12     $D(v) = \min( D(v), D(w) + c(w,v) )$   
13    /* new cost to  $v$  is either old cost to  $v$  or known  
14    shortest path cost to  $w$  plus cost from  $w$  to  $v$  */  
15 until all nodes in  $N$ 
```

# Dijkstra's Algorithm in C

```
#define MAX_NODES 1024          /* maximum number of nodes */
#define INFINITY 1000000000     /* a number larger than every maximum path */
int n, dist[MAX_NODES][MAX_NODES]; /* dist[i][j] is the distance from i to j */

void shortest_path(int s, int t, int path[])
{ struct state {                /* the path being worked on */
    int predecessor;            /* previous node */
    int length;                 /* length from source to this node */
    enum {permanent, tentative} label; /* label state */
} state[MAX_NODES];

int i, k, min;
struct state *p;

for (p = &state[0]; p < &state[n]; p++) { /* initialize state */
    p->predecessor = -1;
    p->length = INFINITY;
    p->label = tentative;
}
state[t].length = 0; state[t].label = permanent;
k = t;                /* k is the initial working node */
```

# Dijkstra's Algorithm in C

```
do {
    /* Is there a better path from k? */
    for (i = 0; i < n; i++)
        /* this graph has n nodes */
        if (dist[k][i] != 0 && state[i].label == tentative) {
            if (state[k].length + dist[k][i] < state[i].length) {
                state[i].predecessor = k;
                state[i].length = state[k].length + dist[k][i];
            }
        }
    }

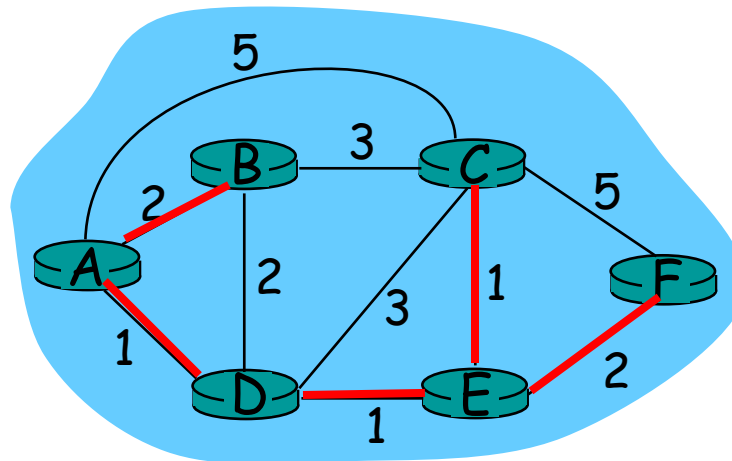
    /* Find the tentatively labeled node with the smallest label. */
    k = 0; min = INFINITY;
    for (i = 0; i < n; i++)
        if (state[i].label == tentative && state[i].length < min) {
            min = state[i].length;
            k = i;
        }
    state[k].label = permanent;
} while (k != s);

/* Copy the path into the output array. */
i = 0; k = s;
do {path[i++] = k; k = state[k].predecessor; } while (k >= 0);
}
```



# Dijkstra's algorithm: example

Step	start N	D(B),p(B)	D(C),p(C)	D(D),p(D)	D(E),p(E)	D(F),p(F)
→ 0	A	2,A	5,A	1,A	infinity	infinity
→ 1	AD	2,A	4,D		2,D	infinity
→ 2	ADE	2,A	3,E			4,E
→ 3	ADEB		3,E			4,E
→ 4	ADEBC					4,E
5	ADEBCF					



# Dijkstra's algorithm, discussion

**Algorithm complexity:** n nodes

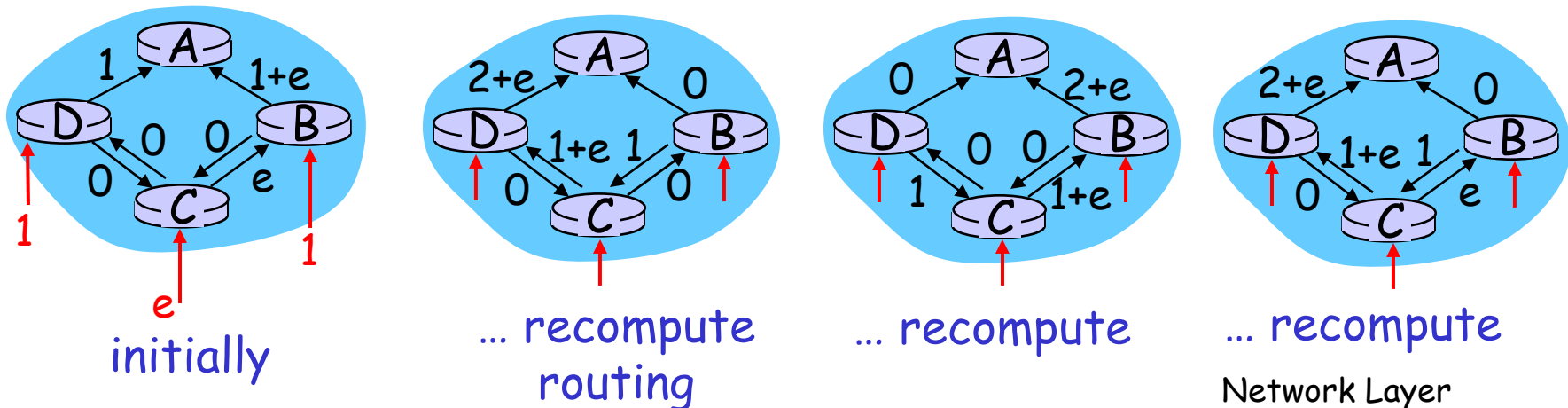
□ each iteration: need to check all nodes, w, not in N

□ 
$$\sum_{i=1}^{n-1} n-i = \frac{n(n+1)}{2} = O(n^2)$$

□ more efficient implementations possible:  $O(n \log n)$

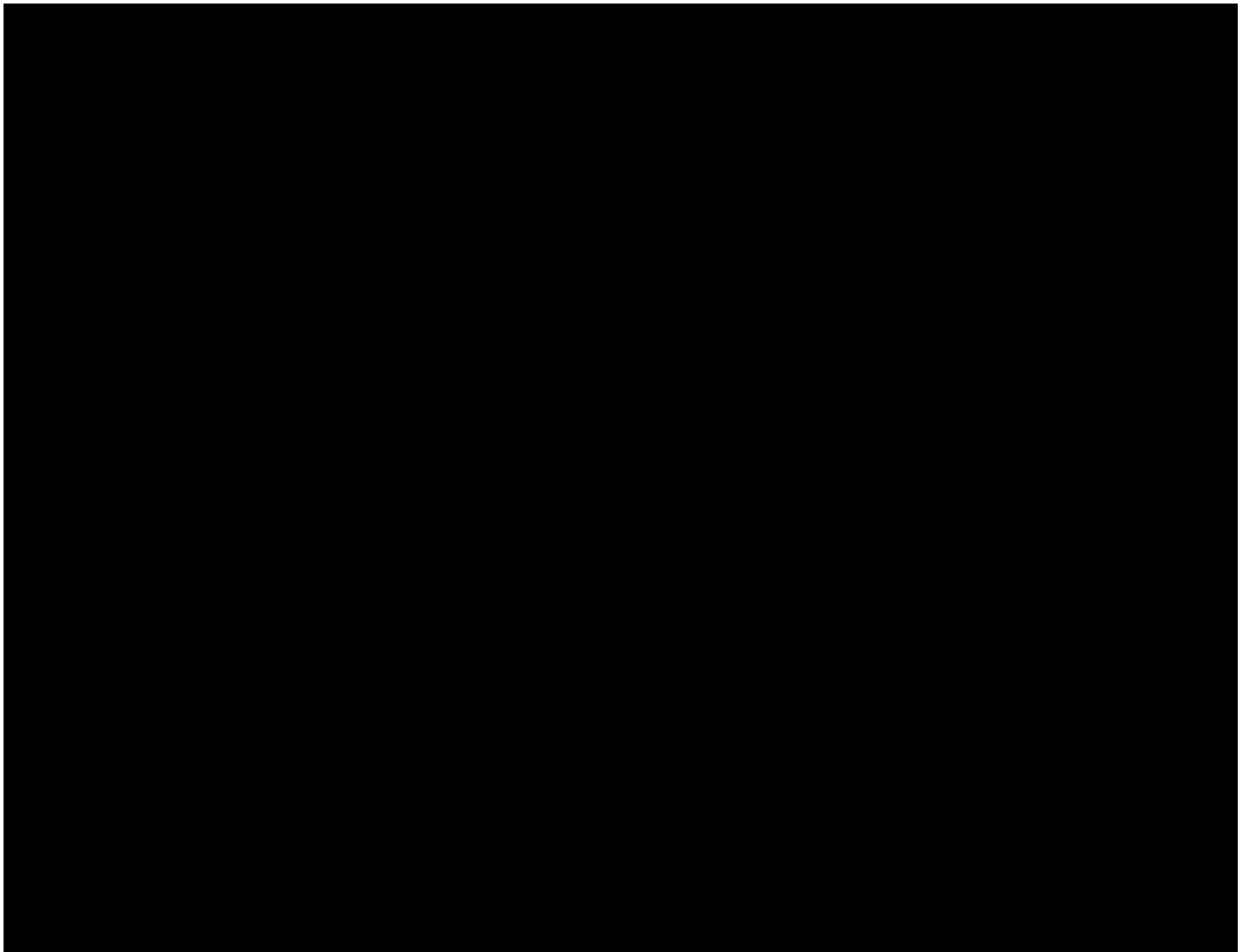
**Oscillations possible:**

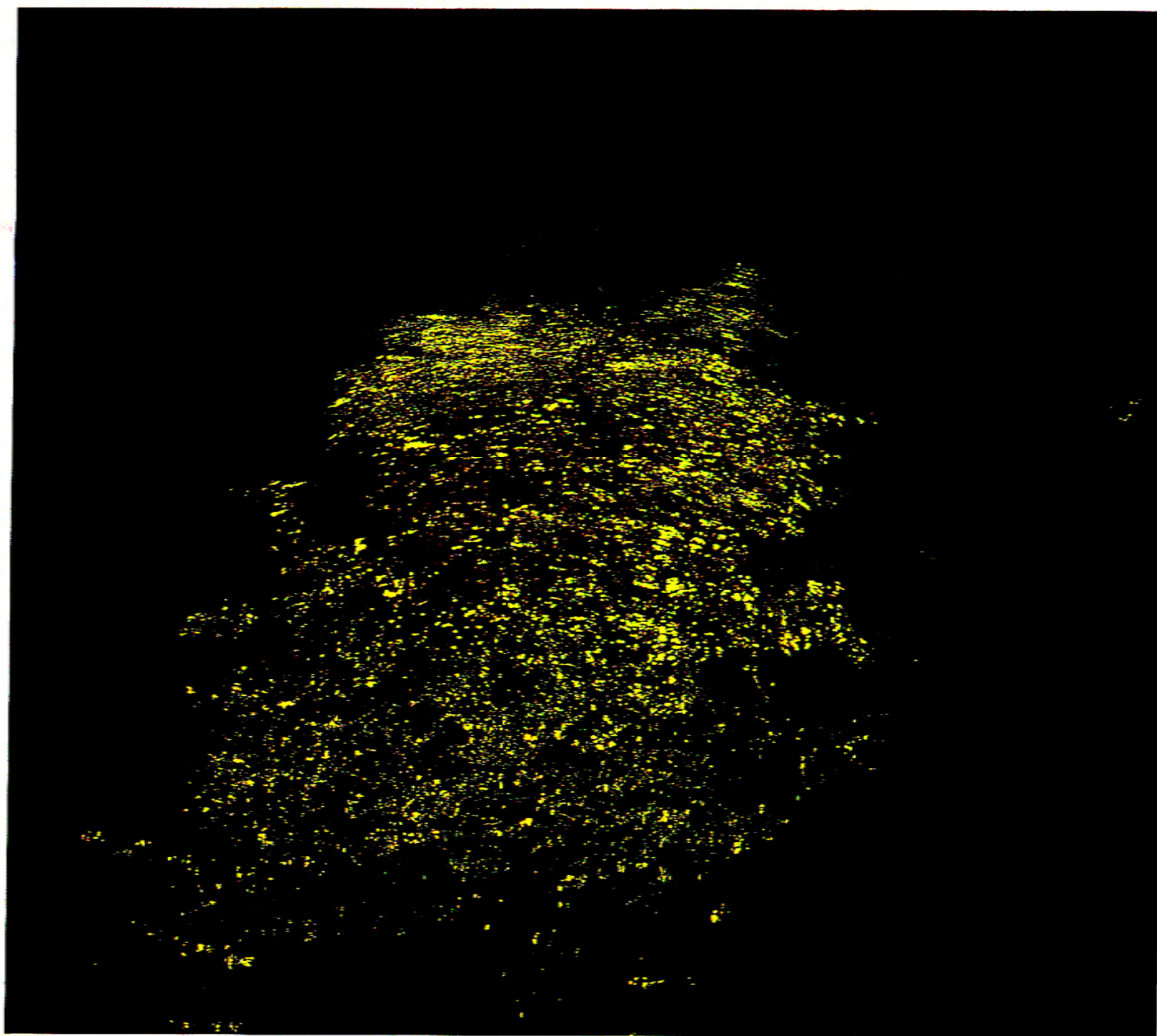
□ e.g., if link cost = amount of carried traffic



# Spontaneous synchronization

- ❑ To avoid oscillations make the routers recompute&send the link costs at different times?
- ❑ Turns out that if the recomputation periodicity is more or less the same on all routers then they eventually synchronize their execution times!
- ❑ The phenomenon of spontaneous synchronization occurs in physics, biology, chemistry, sociology, medicine, etc.





# Shortest Path Routing Summary

Each router does the following:

- Discover its neighbors, learn their network address and UP state (HELLO message)
- Measure the delay or cost to each of its neighbors (ECHO message or cost function)
- Construct a packet telling what it knows (LS message)
- Send this packet to all other routers (every ROUTE REFRESH INTERVAL)
- Compute the shortest path to every other router (Dijkstra)

# Shortest Path Routing Summary

Moreover:

- On every Link State change flood LS to all other routers
- Avoid oscillations through different periods
- Keep LS message counter to keep flooding in check
- Keep LS message age to keep counter in check
- Counter and age also used for fault tolerance