

LECTURE 12: LOGICS FOR MULTIAGENT SYSTEMS

An Introduction to Multiagent Systems

<http://www.csc.liv.ac.uk/~mjw/pubs/imas/>

1 Overview

- The aim is to give an overview of the ways that theorists *conceptualise* agents, and to summarise some of the key developments in agent theory.
- Begin by answering the question: *why theory?*
- Discuss the various different *attitudes* that may be used to characterise agents.
- Introduce some problems associated with formalising attitudes.
- Introduce modal logic as a tool for reasoning about attitudes, focussing on knowledge/belief.
- Discuss Moore's theory of ability.
- Introduce the Cohen-Levesque theory of intention as a case study in agent theory.

2 Why Theory?

- Formal methods have (arguably) had little impact of general practice of software development: why should they be relevant in agent based systems?
- The answer is that we need to be able to give a *semantics* to the architectures, languages, and tools that we use — literally, a *meaning*.
- Without such a semantics, it is never clear exactly *what* is happening, or *why* it works.
- End users (e.g., programmers) need never read or understand these semantics, but progress cannot be made in language development until these semantics exist.

- In agent-based systems, we have a bag of concepts and tools, which are intuitively easy to understand (by means of metaphor and analogy), and have obvious potential.
- But we need theory to reach any kind of *profound* understanding of these tools.

3 Agents = Intentional Systems

- Where do theorists start from?
- The notion of an agent as an *intentional system*...
- So agent theorists start with the (strong) view of agents as intentional systems: one whose simplest consistent description requires the intentional stance.

4 Theories of Attitudes

- We want to be able to design and build computer systems in terms of 'mentalist' notions.
- Before we can do this, we need to identify a tractable subset of these attitudes, and a model of how they interact to generate system behaviour.
- So first, *which* attitudes?

- Two categories:

information attitudes { belief
knowledge

pro-attitudes { desire
intention
obligation
commitment
choice
...

5 Formalising Attitudes

- So how do we formalise attitudes?
- Consider...

Janine believes Cronos is father of Zeus.

- Naive translation into first-order logic:

Bel(Janine, *Father*(Zeus, Cronos))

- But...
 - the second argument to the *Bel* predicate is a *formula* of first-order logic, not a term;
need to be able to apply 'Bel' to formulae;
 - allows us to substitute terms with the same denotation:
consider (*Zeus = Jupiter*)
intentional notions are referentially opaque.

- So, there are two sorts of problems to be addressed in developing a logical formalism for intentional notions:
 - a *syntactic* one (intentional notions refer to sentences); and
 - a *semantic* one (no substitution of equivalents).
- Thus any formalism can be characterized in terms of two attributes: its *language of formulation*, and *semantic model* [?, p83].
- Two fundamental approaches to the syntactic problem:
 - use a *modal* language, which contains *modal operators*, which are applied to formulae;
 - use a *meta-language*: a first-order language containing terms that denote formulae of some other *object-language*.
- We will focus on modal languages, and in particular, *normal modal logics*, with *possible worlds semantics*.

6 Normal Modal Logics

- We introduce a (propositional) modal logic for knowledge/belief.

- Syntax is classical propositional logic, plus an operator K for 'knows that'.

Vocabulary:

$\Phi = \{p, q, r, \dots\}$ primitive propositions
 $\wedge, \vee, \neg, \dots$ classical connectives
 K modal connective

Syntax:

$$\begin{array}{lcl}
 \langle wff \rangle & ::= & \text{any member of } \Phi \\
 & | & \neg \langle wff \rangle \\
 & | & \langle wff \rangle \vee \langle wff \rangle \\
 & | & K \langle wff \rangle
 \end{array}$$

So nesting of K is allowed.

- Example formulae:

$$\begin{array}{l}
 K(p \wedge q) \\
 K(p \wedge Kq)
 \end{array}$$

- Semantics are trickier. The idea is that an agent's beliefs can be characterized as a set of *possible worlds*, in the following way.
- Consider an agent playing a card game such as poker, who possessed the ace of spades.
How could she deduce what cards were held by her opponents?
- First calculate all the various ways that the cards in the pack could possibly have been distributed among the various players.
- The systematically eliminate all those configurations which are *not possible, given what she knows*.
(For example, any configuration in which she did not possess the ace of spades could be rejected.)

- Each configuration remaining after this is a *world*; a state of affairs considered possible, given what she knows.
- Something true in *all* our agent's possibilities is believed by the agent.
For example, in all our agent's *epistemic alternatives*, she has the ace of spades.
- Two advantages:
 - remains neutral on the cognitive structure of agents;
 - the associated mathematical theory is very nice!

- To formalise all this, let W be a set of worlds, and let $R \subseteq W \times W$ be a binary relation on W , characterising what worlds the agent considers possible.
- For example, if $(w, w') \in R$, then if the agent was *actually* in world w , then as far as it was concerned, it *might* be in world w' .
- Semantics of formulae are given relative to worlds: in particular:
 $K\phi$ is true in world w iff ϕ is true in all worlds w' such that $(w, w') \in R$.

- Two basic properties of this definition:
 - the following axiom schema is valid:

$$K(\phi \Rightarrow \psi) \Rightarrow (K\phi \Rightarrow K\psi)$$
 - if ϕ is valid, then $K\phi$ is valid.
- Thus *agent's knowledge is closed under logical consequence*:
 this is *logical omniscience*.
 This is *not* a desirable property!

- The most interesting properties of this logic turn out to be those relating to the properties we can impose on accessibility relation R .

By imposing various constraints, we end up getting out various axioms; there are *lots* of these, but the most important are:

$$\begin{aligned} \text{T} \quad & K\phi \Rightarrow \phi \\ \text{D} \quad & K\phi \Rightarrow \neg K\neg\phi \\ \text{4} \quad & K\phi \Rightarrow KK\phi \\ \text{5} \quad & \neg K\neg\phi \Rightarrow K\neg K\neg\phi. \end{aligned}$$

- Axiom T is the *knowledge axiom*: it says that what is known is true.
- Axiom D is the *consistency axiom*: if you know ϕ , you can't also know $\neg\phi$.
- Axiom 4 is *positive introspection*: if you know ϕ , you know you know ϕ .
- Axiom 5 is *negative introspection*: you are aware of what you don't know.
- We can (to a certain extent) pick and choose which axioms we want to represent our agents.
- All of these (KTD45) constitute the logical system S5.
(Often chosen as a logic of *idealised knowledge*.)
- S5 without the T is weak-S5, or KD45.
(Often chosen as a logic of *idealised belief*.)

7 Knowledge & Action

- Most-studied aspect of practical reasoning agents:

interaction between knowledge and action.

- Moore's 1977 analysis is best-known in this area.
- Formal tools:
 - a modal logic with Kripke semantics + dynamic logic-style representation for action;
 - *but* showed how Kripke semantics could be axiomatized in a first-order meta-language;
 - modal formulae then translated to meta-language using axiomatization;
 - modal theorem proving reduces to meta-language theorem proving.

- Moore considered 2 aspects of interaction between knowledge and action:
 1. As a result of performing an action, an agent can gain knowledge.
Agents can perform “test” actions, in order to find things out.
 2. In order to perform some actions, an agent needs knowledge: these are *knowledge pre-conditions*.
For example, in order to open a safe, it is necessary to know the combination.
- Culminated in defn of *ability*: what it means to be able to do bring something about.

- Axiomatising standard logical connectives:

$$\begin{aligned}
\forall w. True(w, [\neg \phi]) &\Leftrightarrow \neg True(w, [\phi]) \\
\forall w. True(w, [\phi \wedge \psi]) &\Leftrightarrow True(w, [\phi]) \wedge True(w, [\psi]) \\
\forall w. True(w, [\phi \vee \psi]) &\Leftrightarrow True(w, [\phi]) \vee True(w, [\psi]) \\
\forall w. True(w, [\phi \Rightarrow \psi]) &\Leftrightarrow True(w, [\phi]) \Rightarrow True(w, [\psi]) \\
\forall w. True(w, [\phi \Leftrightarrow \psi]) &\Leftrightarrow (True(w, [\phi]) \Leftrightarrow True(w, [\psi]))
\end{aligned}$$

Here, *True* is a meta-language predicate:

- 1st argument is a term denoting a world;
- 2nd argument a term denoting modal language formula.

Frege quotes, $[\]$, used to quote modal language formula.

- Axiomatizing the knowledge connective: basic possible world semantics:

$$\forall w \cdot True(w, [K\phi]) \Leftrightarrow \forall w' \cdot K(w, w') \Rightarrow True(w', [\phi])$$

Here, *K* is a meta-language predicate used to represent the knowledge accessibility relation.

- Other axioms added to represent properties of knowledge.

Reflexive:

$$\forall w. K(w, w)$$

Transitive:

$$\forall w, w', w'' \cdot K(w, w') \wedge K(w', w'') \Rightarrow K(w, w'')$$

Euclidean:

$$\forall w, w', w'' \cdot K(w, w') \wedge K(w'', w') \Rightarrow K(w, w'')$$

These axioms ensure that K is *equivalence relation*.

- Now we need some apparatus for representing *actions*.
- Add a meta-language predicate $R(a, w, w')$ to mean that w' is a world that could result from performing action a in world w .
- Then introduce a modal operator $(\text{Res } a \phi)$ to mean that *after action a is performed, ϕ will be true*.

$$\begin{aligned} \forall w. \text{True}(w, \lceil (\text{Res } a \phi) \rceil) &\Leftrightarrow \\ \exists w' \cdot R(a, w, w') \wedge \forall w'' \cdot R(a, w, w'') &\Rightarrow \text{True}(w'', \lceil \phi \rceil) \end{aligned}$$

- first conjunct says the action is *possible*;
- second says that a necessary consequence of performing action is ϕ .

- Now we can define ability, via modal Can operator.

$$\forall w \cdot \text{True}(w, \lceil (\text{Can } \phi) \rceil) \Leftrightarrow \exists a. \text{True}(w, \lceil (\text{Know } (\text{Res } a \phi)) \rceil)$$

So agent can achieve ϕ if there exists some action a , such that agent knows that the result of performing a is ϕ .

- Note the way a is quantified w.r.t. the Know modality.

Implies agent knows the identity of the action.

Has a “definite description” of it.

(Terminology: a is quantified *de re*.)

- We can weaken the definition, to capture the case where an agent performs an action to find out how to achieve goal.

$$\begin{aligned} \forall w \cdot \text{True}(w, \lceil (\text{Can } \phi) \rceil) \Leftrightarrow \\ \exists a. \text{True}(w, \lceil (\text{Know } (\text{Res } a \phi)) \rceil) \vee \\ \exists a. \text{True}(w, \lceil (\text{Know } (\text{Res } a (\text{Can } \phi))) \rceil) \end{aligned}$$

A circular definition?

No, interpret as a *fixed point*.

- Critique of Moore's formalism:

1. Translating modal language into a first-order one and then theorem proving in first-order language is inefficient.
"Hard-wired" modal theorem provers will be more efficient.
2. Formulae resulting from the translation process are complicated and unintuitive.
Original structure (and hence sense) is lost.
3. Moore's formalism based on possible worlds: falls prey to logical omniscience.
Definition of ability is somewhat vacuous.

- But probably first serious attempt to use tools of mathematical logic (incl. modal & dynamic logic) to bear on rational agency.

8 Intention

- We have *one aspect* of an agent, but knowledge/belief alone does not completely characterise an agents.
- We need a *set* of connectives, for talking about an agent's *pro-attitudes* as well.
- Agent needs to achieve a *rational balance* between its attitudes:
 - should not be *over-committed*;
 - should not be *under-committed*.
- Here, we review one attempt to produce a coherent account of how the components of an agent's cognitive state hold together: the theory of intention developed by Cohen & Levesque.
- Here we mean intention as in...

It is my intention to prepare my slides.

8.1 What is intention?

- Two sorts:
 - *present directed*
 - * attitude to an action
 - * function causally in producing behaviour.
 - *future directed*
 - * attitude to a proposition
 - * serve to coordinate future activity.
- We are here concerned with *future directed* intentions.

Following Bratman (1987) Cohen-Levesque identify seven properties that must be satisfied by intention:

1. Intentions pose problems for agents, who need to determine ways of achieving them.
If I have an intention to ϕ , you would expect me to devote resources to deciding how to bring about ϕ .
2. Intentions provide a 'filter' for adopting other intentions, which must not conflict.
If I have an intention to ϕ , you would expect me to adopt an intention ψ such that ϕ and ψ are mutually exclusive.
3. Agents track the success of their intentions, and are inclined to try again if their attempts fail.
If an agent's first attempt to achieve ϕ fails, then all other things being equal, it will try an alternative plan to achieve ϕ .

In addition. . .

- Agents believe their intentions are possible.
That is, they believe there is at least some way that the intentions could be brought about. (CTL notation: $E\Diamond\phi$).*
- Agents do not believe they will not bring about their intentions.
It would not be rational of me to adopt an intention to ϕ if I believed ϕ was not possible. (CTL notation: $A\Box\neg\phi$.)*

- Under certain circumstances, agents believe they will bring about their intentions.
*It would not normally be rational of me to believe that I **would** bring my intentions about; intentions can **fail**. Moreover, it does not make sense that if I believe ϕ is inevitable (CTL*: $A\Diamond\phi$) that I would adopt it as an intention.*

- Agents need not intend all the expected side effects of their intentions.
If I believe $\phi \Rightarrow \psi$ and I intend that ϕ , I do not necessarily intend ψ also. (Intentions are not closed under implication.)

This last problem is known as the **dentist** problem. I may believe that going to the dentist involves pain, and I may also intend to go to the dentist — but this does not imply that I intend to suffer pain!

- Cohen-Levesque use a *multi-modal logic* with the following major constructs:

(Bel $x \phi$) x believes ϕ

(Goal $x \phi$) x has goal of ϕ

(Happens α) action α happens next

(Done α) action α has just happened

- Semantics are possible worlds.
- Each world is infinitely long linear sequence of states.
- Each agent allocated:
 - *belief accessibility relation* — B
for every agent/time pair, gives a set of belief accessible worlds;
Euclidean, serial, transitive — gives belief logic KD45.

- *goal accessibility relation* — G
for every agent/time pair, gives a set of goal accessible worlds.
Serial — gives goal logic KD.

- A constraint: $G \subseteq B$.

– Gives the following inter-modal validity:

$$\models (\text{Bel } i \phi) \Rightarrow (\text{Goal } i \phi)$$

– A *realism* property — agents *accept the inevitable*.

- Another constraint:

$$\models (\text{Goal } i \phi) \Rightarrow \Diamond \neg (\text{Goal } i \phi)$$

C&L claim this assumption captures following properties:

- agents do not persist with goals forever;
- agents do not indefinitely defer working on goals.

- Add in some operators for describing the structure of event sequences

$\alpha; \alpha'$ α followed by α'

$\alpha?$ ‘test action’ α

- Also add some operators of temporal logic, “ \Box ” (always), and “ \Diamond ” (sometime) can be defined as abbreviations, along with a “strict” sometime operator, Later:

$$\Diamond \alpha \hat{=} \exists x \cdot (\text{Happens } x; \alpha?)$$

$$\Box \alpha \hat{=} \neg \Diamond \neg \alpha$$

$$(\text{Later } p) \hat{=} \neg p \wedge \Diamond p$$

- Finally, a temporal precedence operator, (Before p q).
- First major derived construct is a *persistent* goal.

$$\begin{aligned}
 (P - \text{Goal } x \ p) \hat{=} & \\
 & (\text{Goal } x \ (\text{Later } p)) \quad \wedge \\
 & (\text{Bel } x \ \neg p) \quad \wedge \\
 & \left[\begin{array}{l} \text{Before} \\ ((\text{Bel } x \ p) \vee (\text{Bel } x \ \Box \neg p)) \\ \neg(\text{Goal } x \ (\text{Later } p)) \end{array} \right]
 \end{aligned}$$

- So, an agent has a persistent goal of p if:
 1. It has a goal that p eventually becomes true, and believes that p is not currently true.
 2. Before it drops the goal, one of the following conditions must hold:

- the agent believes the goal has been satisfied;
- the agent believes the goal will never be satisfied.

- Next, intention:

$$(\text{Intend } x \alpha) \hat{=} \\ (\text{P} - \text{Goal } x \\ [\text{Done } x (\text{Bel } x (\text{Happens } \alpha))]; \alpha) \\)$$

- So, an agent has an intention to do α if: it has a persistent goal to have believed it was about to do α , and then done α .
- C&L discuss how this definition satisfies desiderata for intention.
- Main point: avoids *ever commitment*.
- Adaptation of definition allows for *relativised intentions*. Example:
I have an intention to prepare slides for the tutorial, relative to the belief that I will be paid for tutorial. If I ever come to believe that I will not be paid, the intention evaporates. . .

- Critique of C&L theory of intention (Singh, 1992):
 - does not capture an adequate notion of “competence”;
 - does not adequately represent intentions to do composite actions;
 - requires that agents know what they are about to do — fully elaborated intentions;
 - disallows multiple intentions.

9 Semantics for Speech Acts

- C&L used their theory of intention to develop a theory of several speech acts.
- Key observation: illocutionary acts are *complex event types* (cf. actions).
- C&L use their dynamic logic-style formalism for representing these actions.
- We will look at *request*.
- First, define *alternating belief*.

$$(\text{AltBel } n \ x \ y \ p) \hat{=} \underbrace{(\text{Bel } x \ (\text{Bel } y \ (\text{Bel } x \ \cdots (\text{Bel } x \ p) \cdots))}_{n \text{ times}} \underbrace{\cdots)}_{n \text{ times}}$$

- And the related concept of *mutual belief*.

$$(\text{M} - \text{Bel } x \ y \ p) \hat{=} \forall n \cdot (\text{AltBel } n \ x \ y \ p)$$

- An *attempt* is defined as a complex action expression.
(Hence the use of curly brackets, to distinguish from predicate or modal operator.)

$$\{\text{Attempt } x \ e \ p \ q\} \hat{=} \left[\begin{array}{l} (\text{Bel } x \ \neg p) \\ (\text{Goal } x \ (\text{Happens } x \ e; p?)) \\ (\text{Intend } x \ e; q?) \end{array} \wedge \right] ?; e$$

In English:

“An attempt is a complex action that agents perform when they do something (*e*) desiring to bring about some effect (*p*) but with intent to produce at least some result (*q*)”.

Here:

- *p* represents ultimate goal that agent is aiming for by doing *e*;

- proposition *q* represents what it takes to at least make an “honest effort” to achieve *p*.

- Definition of *helpfulness* needed:

$$\begin{aligned}
 (\text{Helpful } x \ y) \hat{=} & \\
 \forall e \cdot & \left[(\text{Bel } x \ (\text{Goal } y \ \diamond (\text{Done } x \ e))) \ \wedge \right. \\
 & \left. \neg(\text{Goal } x \ \Box \neg(\text{Done } x \ e)) \right] \\
 & \Rightarrow (\text{Goal } x \ \diamond (\text{Done } x \ e))
 \end{aligned}$$

In English:

“[C]onsider an agent [x] to be helpful to another agent [y] if, for any action [e] he adopts the other agent’s goal that he eventually do that action, whenever such a goal would not conflict with his own”.

- Definition of *requests*:

$$\begin{aligned}
 \{\text{Request } spkr \ addr \ e \ \alpha\} \hat{=} & \\
 \{ & \text{Attempt } spkr \ e \ \phi \\
 & (\text{M} - \text{Bel } addr \ spkr \ (\text{Goal } spkr \ \phi)) \\
 & \}
 \end{aligned}$$

where ϕ is

$$\begin{aligned}
 & \diamond(\text{Done } addr \ \alpha) \ \wedge \\
 & (\text{Intend } addr \ \alpha \\
 & \left[(\text{Goal } spkr \ \diamond(\text{Done } addr \ \alpha)) \ \wedge \right. \\
 & \left. (\text{Helpful } addr \ spkr) \right] \\
 &)
 \end{aligned}$$

In English:

A request is an attempt on the part of *spkr*, by doing *e*, to bring about a state where, ideally, 1) *addr* intends α , (relative to the *spkr* still having that goal, and *addr* still being helpfully inclined to *spkr*), and 2) *addr* actually eventually does α , or at least brings about a state where *addr* believes it is mutually believed that it wants the ideal situation.

- By this definition, there is no primitive request act:

“[A] speaker is viewed as having performed a request if he executes any sequence of actions that produces the needed effects”.

10 A Theory of Cooperation

- We now move on to a theory of *cooperation* (or more precisely, cooperative problem solving).
- This theory draws on work such as C&L's model of intention, and their semantics for speech acts.
- It uses connectives such as 'intend' as the building blocks.
- The theory intends to explain how an agent can start with an desire, and be moved to get other agents involved with achieving this desire.

11 A(nother) Formal Framework

- We formalise our theory by expressing it in a quantified multi-modal logic.
 - beliefs;
 - goals;
 - dynamic logic style action constructors;
 - path quantifiers (branching time);
 - groups (sets of agents) as terms in the language — set theoretic mechanism for reasoning about groups;
 - actions (transitions in branching time structure) associated with agents.
- Formal semantics in the paper!

12 The Four-Stage Model

1. **Recognition.**

CPS begins when some agent recognises the potential for cooperative action.

May happen because an agent has a goal that it is unable to achieve in isolation, or because the agent prefers assistance.

2. **Team formation.**

The agent that recognised the potential for cooperative action at stage (1) solicits assistance.

If team formation successful, then it will end with a group having a joint commitment to collective action.

3. **Plan formation.**

The agents attempt to negotiate a joint plan that they believe will achieve the desired goal.

4. **Team action.**

The newly agreed plan of joint action is executed by the agents, which maintain a close-knit relationship throughout.

12.1 Recognition

- CPS typically begins when some agent in a has a goal, and recognises the potential for cooperative action with respect to that goal.
 - Recognition may occur for several reasons:
 - The agent is unable to achieve its goal in isolation, due to a lack of resources, but believes that cooperative action can achieve it.
 - An agent may have the resources to achieve the goal, but does not want to use them.
- It may believe that in working alone on this particular problem, it will clobber one of its other goals, or it may believe that a cooperative solution will in some way be better.

- Formally...

$$\begin{aligned} (\text{Potential} - \text{for} - \text{Coop } i \phi) \hat{=} & (\text{Goal } i \phi) \wedge \\ & \exists g \cdot (\text{Bel } i (J - \text{Can } g \phi)) \wedge \\ & \left[\neg(\text{Can } i \phi) \vee \right. \\ & \quad (\text{Bel } i \forall \alpha \cdot (\text{Agt } \alpha i) \wedge \\ & \quad \quad (\text{Achieves } \alpha \phi) \Rightarrow \\ & \quad \quad \left. (\text{Goal } i (\text{Doesnt } \alpha))) \right] \end{aligned}$$

- Note:
 - Can is essentially Moore's;
 - J - Can is a generalization of Moore's
 - (Achieves $\alpha \phi$) is dynamic logic $[\alpha]\phi$;
 - Doesnt means it doesn't happen next.

12.2 Team Formation

- Having identified the potential for cooperative action with respect to one of its goals, a rational agent will solicit assistance from some group of agents that it believes can achieve the goal.
- If the agent is successful, then it will have brought about a mental state wherein the group has a joint commitment to collective action.
- Note that agent cannot guarantee that it will be successful in forming a team; it can only *attempt* it.

- Formally...

$$\begin{aligned} (\text{PreTeam } g \phi i) \hat{=} \\ (M - \text{Bel } g (J - \text{Can } g \phi)) \wedge \\ (J - \text{Commit } g (\text{Team } g \phi i) (\text{Goal } i \phi) \dots) \end{aligned}$$

- Note that:
 - Team is defined in later;
 - J – Commit is similar to J – P – Goal.

- The main assumption concerning team formation can now be stated.

$$\models \forall i \cdot (\text{Bel } i (\text{Potential} - \text{for} - \text{Coop } i \phi)) \Rightarrow \\ A \diamond \exists g \cdot \exists \alpha \cdot (\text{Happens } \{\text{Attempt } i \alpha p q\})$$

where

$$p \hat{=} (\text{PreTeam } g \phi i)$$

$$q \hat{=} (\text{M} - \text{Bel } g (\text{Goal } i \phi) \wedge (\text{Bel } i (\text{J} - \text{Can } g \phi))).$$

12.3 Plan Formation

- If team formation is successful, then there will be a group of agents with a joint commitment to collective action.
- But collective action cannot begin until the group agree on what they will actually do.
- Hence the next stage in the CPS process: plan formation, which involves *negotiation*.
- Unfortunately, negotiation is extremely complex — we simply offer some observations about the weakest conditions under which negotiation can be said to have occurred.

- Note that negotiation may *fail*: the collective may simply be unable to reach agreement.
- In this case, the minimum condition required for us to be able to say that negotiation occurred at all is that *at least one* agent proposed a course of action that it believed would take the collective closer to the goal.
- If negotiation succeeds, we expect a team action stage to follow.

- We might also assume that agents will *attempt to bring about their preferences*.

For example, if an agent has an objection to some plan, then it will attempt to prevent this plan being carried out.

- The main assumption is then:

$$\models (\text{PreTeam } g \phi i) \Rightarrow \\ A \diamond \exists \alpha \cdot (\text{Happens } \{J - \text{Attempt } g \alpha p q\})$$

where

$$\begin{aligned} p &\hat{=} (M - \text{Know } g (\text{Team } g \phi i)) \\ q &\hat{=} \exists j \cdot \exists \alpha \cdot (j \in g) \wedge \\ &\quad (M - \text{Bel } g (\text{Bel } j \\ &\quad (\text{Ags } \alpha g) \wedge (\text{Achieves } \alpha \phi))). \end{aligned}$$

12.4 Team Action

- Team action simply involves the team jointly intending to achieve the goal.
- The formalisation of Team is simple.

$$(\text{Team } g \phi i) \hat{=} \exists \alpha \cdot (\text{Achieves } \alpha \phi) \wedge \\ (\text{J} - \text{Intend } g \alpha (\text{Goal } i \phi))$$