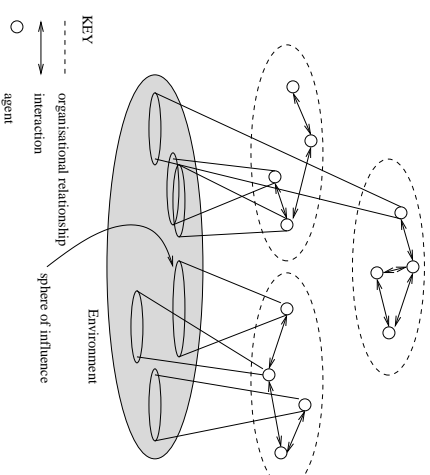


## 1 What are Multiagent Systems?



<http://www.csc.liv.ac.uk/~mjlw/pubs/imas/>

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## LECTURE 6: MULTIAGENT INTERACTIONS

### An Introduction to Multiagent Systems

<http://www.csc.liv.ac.uk/~mjlw/pubs/imas/>

- ... us a multiagent system contains a number of agents ...
- ... which interact through communication ...
- ... are able to act in an environment ...
- ... have different “spheres of influence” (which may coincide)...
- ... will be linked by other (organisational) relationships.

## 2 Utilities and Preferences

- Assume we have just two agents:  $Ag = \{i, j\}$ .
- Agents are assumed to be *self-interested*: they *have preferences over how the environment is*.
- Assume  $\Omega = \{\omega_1, \omega_2, \dots\}$  is the set of “outcomes” that agents have preferences over.

- We capture preferences by *utility functions*:

$$u_i : \Omega \rightarrow \mathbb{R}$$

$$u_j : \Omega \rightarrow \mathbb{R}$$

- Utility functions lead to *preference orderings* over outcomes:

$$\omega \succeq_i \omega' \text{ means } u_i(\omega) \geq u_i(\omega')$$

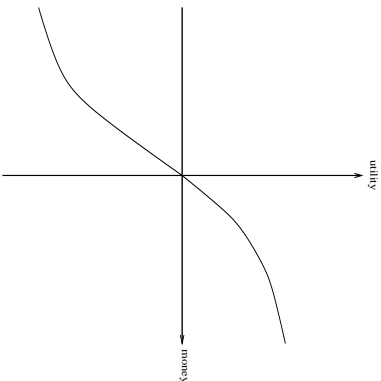
$$\omega \succ_i \omega' \text{ means } u_i(\omega) > u_i(\omega')$$

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### What is Utility?

- Utility is *not* money (but it is a useful analogy).
- Typical relationship between utility & money:



- Here is a state transformer function:

$$\tau(D, D) = \omega_1 \quad \tau(D, C) = \omega_2 \quad \tau(C, D) = \omega_3 \quad \tau(C, C) = \omega_4$$

- (This environment is sensitive to actions of both agents.)

- Here is another:

$$\tau(D, D) = \omega_1 \quad \tau(D, C) = \omega_1 \quad \tau(C, D) = \omega_1 \quad \tau(C, C) = \omega_1$$

- (Neither agent has any influence in this environment.)

- And here is another:

$$\tau(D, D) = \omega_1 \quad \tau(D, C) = \omega_2 \quad \tau(C, D) = \omega_1 \quad \tau(C, C) = \omega_2$$

- (This environment is controlled by  $j$ .)

### 3 Multiagent Encounters

- We need a model of the environment in which these agents will act...
- agents simultaneously choose an action to perform, and as a result of the actions they select, an outcome in  $\Omega$  will result;
- the *actual* outcome depends on the *combination* of actions;
- assume each agent has just two possible actions that it can perform  $C$  ("cooperate") and " $D$ " ("defect").
- Environment behaviour given by *state transformer function*:

$$\tau : \underbrace{A_C}_{\text{agent } i\text{'s action}} \times \underbrace{A_C}_{\text{agent } j\text{'s action}} \rightarrow \Omega$$

### Rational Action

- Suppose we have the case where *both* agents can influence the outcome, and they have utility functions as follows:

$$\begin{array}{llll} u_i(\omega_1) = 1 & u_i(\omega_2) = 1 & u_i(\omega_3) = 4 & u_i(\omega_4) = 4 \\ u_j(\omega_1) = 1 & u_j(\omega_2) = 4 & u_j(\omega_3) = 1 & u_j(\omega_4) = 4 \end{array}$$

- With a bit of abuse of notation:

$$\begin{array}{llll} u_i(D, D) = 1 & u_i(D, C) = 1 & u_i(C, D) = 4 & u_i(C, C) = 4 \\ u_j(D, D) = 1 & u_j(D, C) = 4 & u_j(C, D) = 1 & u_j(C, C) = 4 \end{array}$$

- Then agent  $i$ 's preferences are:

$$C, C \succeq_i C, D \succ_i D, C \succeq_i D, D$$

- " $C$ " is the *rational choice* for  $i$ .

(Because  $i$  prefers all outcomes that arise through  $C$  over all outcomes that arise through  $D$ .)

### Payoff Matrices

- We can characterise the previous scenario in a *payoff matrix*

		$i$	
		defect	coop
$j$	defect	1 4	1 4
	coop	1 4	4 4

- Agent  $i$  is the *column player*.
- Agent  $j$  is the *row player*.

### Nash Equilibrium

- In general, we will say that two strategies  $s_1$  and  $s_2$  are in Nash equilibrium if:
  1. under the assumption that agent  $i$  plays  $s_1$ , agent  $j$  can do no better than play  $s_2$ ; and
  2. under the assumption that agent  $j$  plays  $s_2$ , agent  $i$  can do no better than play  $s_1$ .
- *Neither agent has any incentive to deviate from a Nash equilibrium.*
- Unfortunately:
  1. *Not every interaction scenario has a Nash equilibrium.*
  2. *Some interaction scenarios have more than one Nash equilibrium.*

### Dominant Strategies

- Given any particular strategy  $s$  (either  $C$  or  $D$ ) agent  $i$ , there will be a number of possible outcomes.
- We say  $s_1$  *dominates*  $s_2$  if every outcome possible by  $i$  playing  $s_1$  is preferred over every outcome possible by  $i$  playing  $s_2$ .
- A rational agent will never play a dominated strategy.
- So in deciding what to do, we can *delete dominated strategies*.
- Unfortunately, there isn't always a unique undominated strategy.

### Competitive and Zero-Sum Interactions

- Where preferences of agents are diametrically opposed we have *strictly competitive* scenarios.
- Zero-sum encounters are those where utilities sum to zero:
 
$$u_i(\omega) + u_j(\omega) = 0 \quad \text{for all } \omega \in \Omega.$$
- Zero sum implies strictly competitive.
- Zero sum encounters in real life are very rare ... but people tend to act in many scenarios as if they were zero sum.

#### 4 The Prisoner's Dilemma

Two men are collectively charged with a crime and held in separate cells, with no way of meeting or communicating.

They are told that:

- if one confesses and the other does not, the confessor will be freed, and the other will be jailed for three years;
- if both confess, then each will be jailed for two years.

Both prisoners know that if neither confesses, then they will each be jailed for one year.

- The *individual rational* action is *defect*.

This guarantees a payoff of no worse than 2, whereas cooperating guarantees a payoff of at most 1.

- So defection is the best response to all possible strategies: both agents defect, and get payoff = 2.

- But *intuition* says this is *not* the best outcome:

Surely they should both cooperate and each get payoff of 3!

- Payoff matrix for prisoner's dilemma:

		$i$	
		defect	coop
$j$	defect	2    1	4    1
	coop	1    4	3    3

- Top left: If both defect, then both get punishment for mutual defection.
- Top right: If  $i$  cooperates and  $j$  defects,  $i$  gets sucker's payoff of 1, while  $j$  gets 4.
- Bottom left: If  $j$  cooperates and  $i$  defects,  $j$  gets sucker's payoff of 1, while  $i$  gets 4.
- Bottom right: Reward for mutual cooperation.

- This apparent paradox is *the fundamental problem of multi-agent interactions*.

It appears to imply that *cooperation will not occur in societies of self-interested agents*.

- Real world examples:
  - nuclear arms reduction (“why don’t I keep mine...”)
  - free rider systems — public transport;
  - in the UK — television licenses.
- The prisoner's dilemma is *ubiquitous*.
- Can we recover cooperation?

## Arguments for Recovering Cooperation

- Conclusions that some have drawn from this analysis:
  - the game theory notion of rational action is wrong!
  - somehow the dilemma is being formulated wrongly
- Arguments to recover cooperation:
  - We are not all machiavelli!
  - The other prisoner is my twin!
  - The shadow of the future...

## 4.2 Backwards Induction

- But... suppose you both know that you will play the game exactly  $n$  times.  
On round  $n - 1$ , you have an incentive to defect, to gain that extra bit of payoff...  
But this makes round  $n - 2$  the last "real", and so you have an incentive to defect there, too.  
This is the *backwards induction* problem.
- Playing the prisoner's dilemma with a fixed, finite, pre-determined, commonly known number of rounds, defection is the best strategy.

## 4.1 The Iterated Prisoner's Dilemma

- One answer: *play the game more than once*.  
If you know you will be meeting your opponent again, then the incentive to defect appears to evaporate.
- *Cooperation is the rational choice in the infinitely repeated prisoner's dilemma.*  
(Hurrah!)

## 4.3 Axelrod's Tournament

- Suppose you play iterated prisoner's dilemma against a *range* of opponents ...  
What strategy should you choose, so as to maximise your overall payoff?
- Axelrod (1984) investigated this problem, with a computer tournament for programs playing the prisoner's dilemma.

### Strategies in Axelrod's Tournament

- ALLD: "Always defect" — the *hawk* strategy;
- TIT-FOR-TAT:
  1. On round  $u = 0$ , cooperate.
  2. On round  $u > 0$ , do what your opponent did on round  $u - 1$ .
- TESTER: On 1st round, defect. If the opponent retaliated, then play TIT-FOR-TAT. Otherwise intersperse cooperation & defection.
- JOSS: As TIT-FOR-TAT, except periodically defect.

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### 5 Game of Chicken

- Consider another type of encounter — the *game of chicken*:

		$j$	
		defect	coop
$i$	defect	1	2
	coop	4	3

- (Think of James Dean in *Rebel without a Cause*: swerving = coop, driving straight = defect.)

- Difference to prisoner's dilemma:

*Mutual defection is most feared outcome.*

- (Whereas sucker's payoff is most feared in prisoner's dilemma.)

- Strategies (c,d) and (d,c) are in Nash equilibrium

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### Recipes for Success in Axelrod's Tournament

Axelrod suggests the following rules for succeeding in his tournament:

- *Don't be envious*: Don't play as if it were zero sum!
- *Be nice*: Start by cooperating, and reciprocate cooperation.
- *Retaliate appropriately*: Always punish defection immediately, but use "measured" force — don't overdo it.
- *Don't hold grudges*: Always reciprocate cooperation immediately.

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### 6 Other Symmetric 2 x 2 Games

- Given the 4 possible outcomes of (symmetric) cooperate/defect games, there are 24 possible orderings on outcomes.
  - $CC \succ_i CD \succ_i DC \succ_i DD$   
*Cooperation dominates.*
  - $DC \succ_i DD \succ_i CC \succ_i CD$   
*Deadlock*. You will always do best by defecting.
  - $DC \succ_i CC \succ_i DD \succ_i CD$   
*Prisoner's dilemma.*
  - $DC \succ_i CC \succ_i CD \succ_i DD$   
*Chicken.*
  - $CC \succ_i DC \succ_i DD \succ_i CD$   
*Stag hunt.*

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