

# Spatial Dynamics of Indoor Radio Wideband Channels

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**Abstract**—The multipath components of super-wideband (2-17.2 GHz) non line of sight channel responses measured inside several buildings are stable along sections that are 27 cm long on average with a standard deviation of 16 cm. The stability regions of multipath components have an approximately log-normal histogram. An analysis of measured channels that explicitly includes finite spatial areas of visibility of the multipath components is superior to the classic analysis that attributes spatial dynamics to interference of the multipath. The spatial stability of measured responses, i.e. the size of the typical area of visibility of each multipath component, decreases as the carrier frequency increases but does not depend on bandwidth. The results offer insight into the nature of the diffuse part of the radio channel.

## I. INTRODUCTION

The temporal dynamics of radio channels are intimately related to their variation in space. Temporal channel variation is usually attributed either to movement of the terminals, as in the case of a mobile telephone held while walking, or movement of objects in the environment of the communications system.

The analysis of measured or simulated wideband channels is normally carried out in the time domain, i.e. in the form of impulse responses. The angle of arrival of each multipath component, together with the motion of the receiving antenna, determines the shift in path arrival time as the receiver moves. The Doppler shift of a multipath component is a frequency domain concept; it is manifested in the impulse response by a location-dependent time of arrival of the multipath components. The spread of Doppler shifts of the different components that constitute a whole channel response is often thought to be the main cause of channel variation in space or time.

The classical description of channel dynamics in time is the coherence period, that characterizes the typical period where the channel tends to be more or less constant. In the classic channel model, the coherence period is inversely related to the Doppler spread of the response. Channel analysis that is based on the Doppler spread implicitly assumes that each multipath component is received over the entire region of receiver locations [1]. We test this assumption using a large measurement campaign to find that it is not realistic even for decimeter scale regions.

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This research was supported by The Israel Science Foundation (Grant No. 249/06), the Israeli Short Range Consortium (ISRC) and NEWCOM++.

Partial results published in IEEE VTC 2009-Spring, based on a different MPC extraction method.

The common view of multipath channels assumes that spatial dynamics are caused by the interference of multipath components. We tested this assumption by comparing two reconstructions of measured impulse responses based on extracted multipath components; in the ‘unbounded’ reconstruction each component was present along the entire (one-meter) range of receiver locations and in the ‘bounded’ reconstruction they had finite areas of visibility. The results indicate that interference of stable multipath components gives a significantly inferior reconstruction of the channel when compared with a reconstruction that attributes to each path a limited area of visibility.

The results show a clear decrease, in the average and in the standard deviation of the length of the visibility area, as the carrier frequency increases in the range 2 GHz to 17 GHz. We conclude that the channel is spatially more stable at lower bands. The apparent stability of the multipath components is unaffected by variation of the bandwidth between 100 MHz and 1.5 GHz.

A possible explanation follows the idea of ‘wideband Fresnel zones’ suggested in [2], [3], [4], [5]. In particular, [5] suggests a Fresnel zone analysis that predicts effective areas of scattering off objects that decrease in size as the carrier frequency increases. The reduction in the effective area of scattering causes a reduction in the range of receiver locations where each multipath component is apparent.

Channel stability has significant implications on various aspects of system design. In particular, multiple antenna (MIMO) systems benefit from small scale channel variation over space, because variations in the channel mean that the different links (between one transmit antenna and one receive antenna) are uncorrelated even if the antennas at each terminal are close to each other.

Our analysis shows average multipath component visibility lengths on the order of a few decimeters. Results from [6] measured correlation lengths of 5-15 cm; Other related work has concentrated on the correlation of path amplitudes [7], [8] as they vary along space, and on the predictability of path amplitude values [9]. Our work is unique as it focuses on the existence of individual paths in adjacent areas in space. Instead of assuming that paths are stable and investigating the evolution of their amplitudes in space, we analyze the appearance of paths as the receiver moves.

Recent MIMO channel models that rely on indoor channel measurements include the spatial dynamics of multipath clusters via birth and death processes. A model based on measurements with a bandwidth of 80 MHz [10] is presented in [11], this bandwidth does not allow inspection of the dynamics of

individual multipath components. Another MIMO model that includes cluster birth and death dynamics is presented in [12]. The measurements used to validate this model were taken with a bandwidth of 200 MHz.

Most models of radio channels, i.e. the 3GPP Spatial Channel Model [13], IEEE 802.11n [14] and the WINNER model [15], [16], [17], do not include the effects of movement of the terminals in space. The models describe the spatial dependence of the channel via angles of departure and angles of arrival of the propagating waves from the transmitter and to the receiver. The spatial dynamic aspect is sometimes described via correlations or coherence distances of various channel parameters.

The COST 259 model [18], [19] describes ‘visibility regions’ for clusters of multipath components in macrocell (outdoor) environments. The model indicates the probability distribution function of the location of the visibility regions. A separate set of visibility regions is randomly generated for each cluster.

For picocell (indoor) environments the COST 259 model describes the birth and death of multipath components using the Poisson process following the work of *Zwick* and collaborators [20]. The spatial dynamics of indoor radio channels were measured with a 120 MHz bandwidth and modelled by *Chong et al.* [21], [22] and *Herdin* [23], and with a 30 MHz bandwidth by *Nielsen et al.* [24]. Spatial dynamics due to blocking of the LoS by people is discussed in [25], and spatial variations of shadowing are shown in indoor–outdoor channels in [26].

## II. MEASUREMENT ENVIRONMENT AND EQUIPMENT

### A. The System

The measurement setup was based on an Agilent N5230 network analyzer, connected to two omni-directional antennas (Electro-Metrics EM-6865) in the 1-18 GHz band with suitable amplifiers. The receive antenna was placed on a meter long linear motorized positioner with sub-millimeter accuracy that was moved between measurements but was kept immobile during the collection of each channel response. The transmit antenna was placed on a cart that was moved to different locations for different measurements, but was immobile during each measurement. Measurements were normally performed during nights, when movement of people around the system was minimal. One antenna was characterized in an anechoic chamber to verify its response.

Calibration was performed using measured responses of the cables and amplifiers, i.e. their responses were removed from the channel responses used for analysis. The (mild) frequency dependent responses of the antennas were also removed, but we could not compensate for the slight deviation of the antenna patterns from the nominal omni-directional pattern. We also did not attempt to compensate for the vertical pattern of the antennas.

We tested the effect of the metallic receiver cart in two ways, by (1) comparing measurements with the cart covered with absorbing material to measurements taken with the cart exposed, and (2) by comparing measurements with the cart

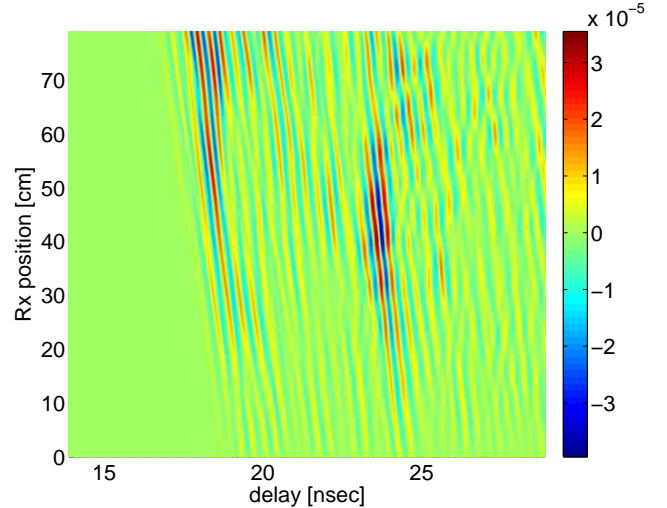


Fig. 1. An example of measured impulse responses. The horizontal axis has delay and the vertical receiver positions. The responses are real with amplitudes that are shown in color. This measurement was taken with terminal separation of 9.8 m, and is typical of near line of sight situations. The color reflects linear amplitude values that may be negative.

direction reversed (rotated by  $180^\circ$ ). No significant effects were seen.

### B. The Measurement Environment

The 50 measurements used in this paper were collected between 2006 and 2008 in four office buildings in the Givat Ram campus of the Hebrew University in Jerusalem and in the Holon Institute of Technology, these buildings have a standard cement and cement block construction. We kept the equipment in a single floor of each building in most of the measurements, and separated them to adjacent floors in five measurements. Transmitter–receiver separation ranged from 3 to 28 meters. All measurement were non line of sight (NLoS).

## III. ANALYSIS

The analysis is based on estimating the individual multipath components, and it focuses on their spatial area of visibility. A *measurement* in this work is a collection of responses measured with a stationary transmitter, and a receiver located at positions that were uniformly spread over a one-meter rail in steps of 2 to 10 mm. The receiver was held stationary during the measurement of each impulse response.

We analyze the measured channel responses using a raised cosine window with 3 dB points at 2 GHz and 17.2 GHz and  $\beta = 0.1$  for the full-band results (Section IV-A) and 3 dB bands of 1 GHz in Section IV-B. After filtering, the measured responses were converted to the time (delay) domain with a 28 psec time step, to generate a two-dimensional real representation of the channel as shown in the example in Figure 1. The channel measurement matrix  $\mathbf{M}$  has rows that span a single channel impulse response, the columns span receiver positions. The delay range was set at 150 nsec around the maximal (absolute) response at one end of the rail, this

seemed sufficient to include all the significant parts of the response.

The temporal resolution of 28 psec was maintained in all our analyses, i.e. responses with bandwidths of 1 GHz are heavily over-sampled. Due to the over-sampling, apparent multipath components with similar delays are correlated.

All the measurements included in this analysis were of sufficient SNR, i.e. at least 13 dB, and above 20 dB most cases (42 of out 50). To calculate the SNR we used the maximum (absolute) amplitude among the multipath components, and normalized its square by the noise variance, calculated from a late 5 nsec section of the response over all the available receiver positions.

A significant feature of our measurements is the finite, and usually short, spatial extent of the multipath components. Figure 1 is typical in this sense, this feature can be seen also in channel responses presented in [27], Figures 10.b and 11.b. The diagonals extend 10 – 60 cm over receiver positions in Figure 1. Line of sight (LoS) measurements have more stable direct components that extend beyond the one meter measured length.

Our analysis is based on a software tool designed to extract the multipath components from the measurements. This tool received measured impulse responses of the type shown in Figure 1 and returned a list of diagonals, each defined by its endpoints, its width and a constant real (possibly negative) amplitude. A brief overview of multipath extraction tools follows, and then a description of our multipath extraction tool.

#### A. Wideband Multipath Extraction

The CLEAN algorithm was introduced from radio astronomy into the analysis of UWB measured channels by *Cramer* [28] and coauthors [29], [30]. CLEAN is essentially an iterative search for the strongest multipath component in channel responses from a single transmitter measured at an array of receivers. The algorithm receives (temporal) impulse responses as input, it searches over delay and angles of arrival, and iteratively removes the strongest MPC from the measurement data until the remaining data is weak enough. *Liu et al.* [31] suggest a modification that accounts for distortion, based on the usage of multiple templates of the received pulse shape.

The SAGE (Space-Alternating Generalized Expectation-maximization) Algorithm was introduced for radio channel analysis by *Fleury et al.* [32], [33] for the extraction of delay and angle of arrival from narrowband and wideband signals. The extension to UWB and the addition of successive cancellation into SAGE were suggested by *Chong et al.* [34] (FD-SAGE) and *Haneda & Takada* [35] (UWB-SAGE). The FD-SAGE algorithm was further enhanced in [36] from SIMO to MIMO settings.

RIMAX [37] is an algorithm similar to SAGE in the fact it iterates over the MPC parameters, RIMAX is based on an improved gradient based parameter estimation that operates simultaneously over the entire set of parameters. It iterates between the specular and the diffuse components of the channel.

An extension RIMAX that is based on an extended Kalman Filter was suggested by [38]. The Kalman Filter utilizes a state-space approach on top of RIMAX and tracks parameters over successive measurement locations. The introduction of the state-space approach made it possible to derive parameters faster than conventional high-resolution algorithms (including RIMAX) since the parameter estimates at one terminal location were used as the initial values for estimates at adjacent terminal locations. This approach extracts long MPCs sustained over a sufficiently large area of terminal locations and attributes other parts of the channel response to the diffuse component. A high-resolution algorithm of this family for ultrawideband signals was presented in [39] and a path tracking mechanism was introduced in [40], that says that ‘significant paths constantly exist in many (terminal) positions’ and attempts to estimate only such MPCs.

The method used in the current work is based on a non-parametric search for energetic sections in the two-dimensional (spatial-temporal) channel response matrix. No assumptions are made on the channel model, and only two threshold parameters are used.

*Santos, Karedal et al.* [41], [42] recently presented a frequency based algorithm that searches over reflector positions, and uses successive cancellation, it is different from CLEAN and SAGE in two significant points: (1) Each MPC may be received at delays that can vary non-linearly over a linearly spaced receiver array, and (2) Each MPC may be received over part of the receiver array.

Our method is similar to that of *Santos et al.* in that it allows for MPCs that impinge over parts of the receiver array. The significant new feature is the millimetric resolution that enables a detailed study of the spatial structure of individual MPCs. The work offered by *Santos et al.* investigated outdoor responses measured with a spatial resolution of 4.8 cm and concentrated on clustered MPCs from distinct reflectors.

#### B. A Simple Multipath Extraction Algorithm

**Input:** The algorithm receives a matrix  $\mathbf{M}_{N_x \times N_t}$  of measured impulse responses, where each row includes a single impulse response. It also receives two vectors: A vector of receiver positions  $\{x_i\}_{i=1}^{N_x}$  with uniformly spaced positions, and a vector of delays  $\{t_j\}_{j=1}^{N_t}$  with uniformly spaced delays. In our data the spatial resolution  $\delta x$  varies between 2 mm and 10 mm for different measurements, and the temporal resolution  $\delta \tau$  equals 28 psec.

In the following description we refer to the  $(i, j)$  position in matrices as the  $(x_i, t_j)$  position, in order to maintain the physical significance of the indices.

Two control parameters are given: a minimal spatial extent of  $D_{\min}$  set to 4 cm, and an amplitude threshold  $Thr$  set at 0.1 (-20 dB).

**Initialization:** Set to zero all points in  $\mathbf{M}$  with an absolute value below a threshold set at  $\max \text{abs}(\mathbf{M}) \times Thr$ . Set to zero a matrix  $\mathbf{I}$  with dimensions  $N_x \times N_t$ , that will be used to indicate which pixels were processed.

**MPC Extraction:** For each location  $x_i$ , for each delay  $t_j$ : If  $\mathbf{I}(x_i, t_j) = 1$ , i.e. the  $(x_i, t_j)$  pixel in the matrix  $\mathbf{M}$  was

already checked, continue to the next pixel (next step of the for loop). If  $M(x_i, t_j) = 0$  continue to the next pixel.

Set  $I(x_i, t_j) = 1$  to indicate that the current pixel was checked. Collect an environment of pixels around  $(x_i, t_j)$  where  $M$  is non-zero and has the same sign as  $M(x_i, t_j)$ . Pixels are collected iteratively by searching over adjacent neighbors (in position or delay) to pixels already collected. For every pixel checked set to zero the corresponding cell in the matrix  $I$ .

After having collected a set of pixels around  $(x_i, t_j)$  approximate it by a parallelogram (over delay and receiver positions) and calculate its effective amplitude. If the resulting parallelogram extends at least  $D_{\min}$  over receiver locations, save it as an estimated MPC. Otherwise reject it.

**Output:** A list of parallelograms over receiver position and delay, each with a signed amplitude.

#### IV. RESULTS

Section IV-A compares full-band (2-17.2 GHz) measurement matrices to their reconstruction based on the multipath components extracted from them. The motivation is a comparison of two types of reconstruction, one of them incorporating multipath components with bounded areas of visibility at the receiver. Section IV-B investigates the apparent visibility of the multipath components in responses with different carrier frequencies.

Investigation of the measured channel responses vs. bandwidth, with different carriers and bandwidth between 100 MHz and 1.5 GHz showed no significant dependence of the visibility length of MPCs on bandwidth.

##### A. Full Band Results

We compare two types of reconstruction of measured impulse responses, both based on the multipath components extracted from them. The *Bounded* Multipath Component Reconstruction as the example in Figure 2, is a reconstruction of a measurement matrix based on multipath components that are present over finite areas of space. The *Unbounded* Multipath Components Reconstruction as the example in Figure 3, is a reconstruction of a measurement matrix that includes multipath components present over the *entire* range of receiver locations. The unbounded reconstruction corresponds to the classic viewpoint, that attributes the spatial dynamics of the channel to the space-dependent delay of the components and to interference between multipath components that are individually stable.

The amplitude of each multipath component in the unbounded reconstruction was calculated from the amplitude given by the extraction software tool using  $A_{UB} = A_B \frac{L_B}{L_{UB}}$  where  $A_B$  is the amplitude returned by the extraction tool (see Section III-B),  $L_B$  is the spatial extent of the diagonal and  $L_{UB}$  is the length of the entire receiver range, usually one meter. This choice of amplitude is best in the sense that the square error between the two types of reconstruction is minimal.

The figure of merit we use to appreciate the two types of reconstruction is the normalized squared error (SE), i.e. the

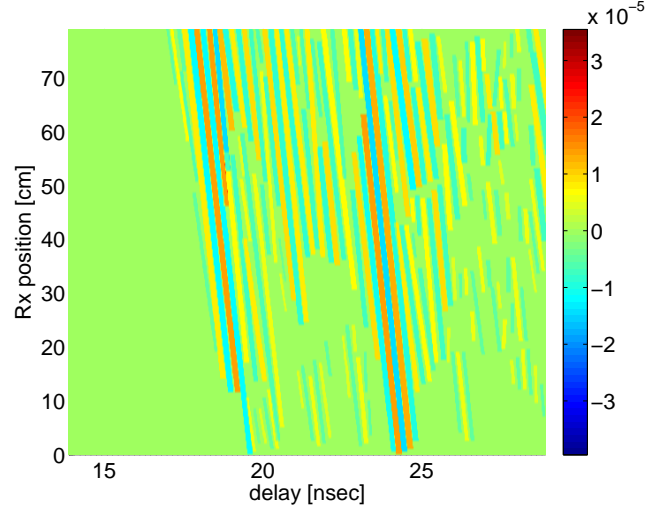


Fig. 2. Bounded multipath components reconstruction of the measurement from Figure 1. In this reconstruction multipath components are represented by diagonals with a fixed amplitude and a finite extent in the delay domain and in receiver locations.

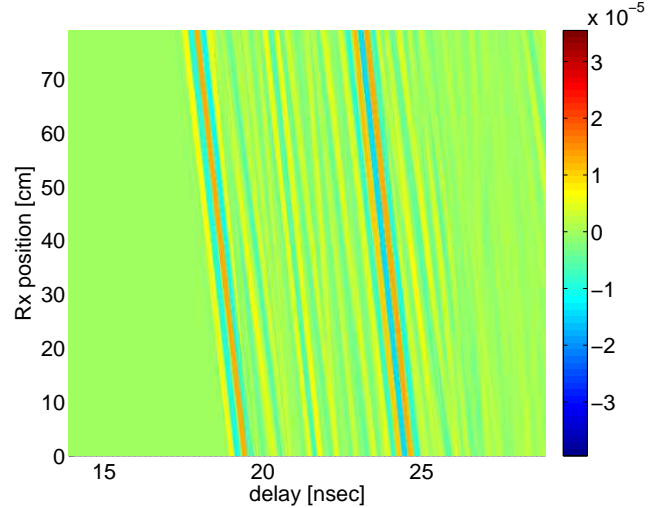


Fig. 3. Unbounded multipath components reconstruction of the measurement from Figure 1. In this reconstruction multipath components are represented by diagonals with a fixed amplitude that extend along the entire range of receiver locations. Note the interference between multipath components over the later delays.

squared difference between a measurement and its reconstruction, summed over receiver locations and delay values and normalized by the energy (sum of squares) of the measured data:

$$SE = \frac{\sum_{\text{Rx Positions}} \sum_{\text{delay}} (\text{meas'd responses} - \text{reconstruction})^2}{\sum_{\text{Rx Positions}} \sum_{\text{delay}} (\text{meas'd responses})^2}$$

Figure 4 presents the squared error of the entire set of measurements with the two types of reconstructions. The unbounded reconstruction is inferior to the bounded one in terms of squared error, and the difference averages (over the set of measurements) to 0.25.

The results are based on the multipath components account-

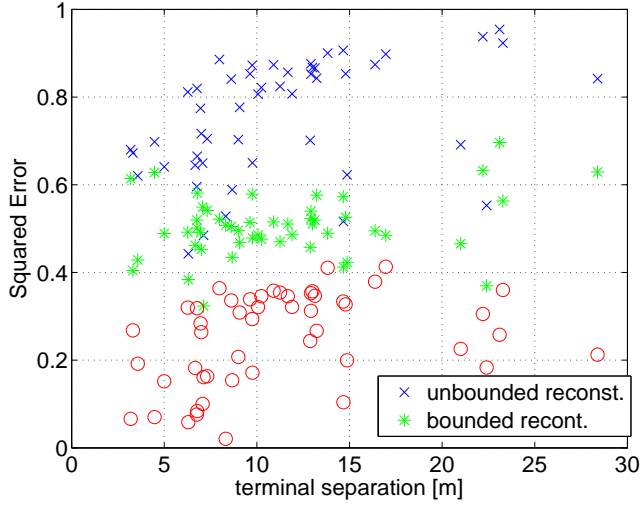


Fig. 4. Performance of channel reconstruction based on the extracted multipath components. The axes show squared error results of the unbounded multipath components reconstruction. The stars show results of the bounded multipath components reconstruction, and the circles show the difference of squared error between the two types of reconstruction. The bounded multipath components reconstruction is superior as it achieves lower squared error.

ing for 80% of the energy of the bounded reconstruction. We calculated the per-measurement mean and standard deviation of the length of these components and the results, averaged over the entire set of measurements, show an average path visibility of 26.5 cm, with a standard deviation of 16.0 cm. The average number of significant multipath components visible from each receiver location<sup>1</sup> is 42.5.

A histogram of the visibility length of the MPC extracted from all the measurements, that account for 80% of the channel energy is shown in Figure 5. The log-normal distribution is a very good fit, with mean 13.6 cm and standard deviation 7.1 cm.

### B. Sub-Band Results - Carrier Dependence

The investigation described in this section focuses on the apparent size of the visibility areas of the multipath components, where the measured responses were filtered to different 1 GHz-wide bands. We show that the visibility areas tend to shrink as the carrier frequency increases.

The measured channel responses were filtered using a raised cosine window with 3 dB-bandwidth of 1 GHz and  $\beta = 0.1$ . The responses measured per each receiver location along the rail were then converted to the time (delay) domain, to generate a two-dimensional representation of the channel as shown in the example in Figure 6. Figure 7 shows the measurement from Figure 6 in a different band.

An example of the average diagonal length against sub-band center frequency is shown in Figure 8, along with the standard deviation. This example is typical in the sense that it shows a reduction of the mean and standard deviation of the

<sup>1</sup>We corrected the apparent number of multipath components to account for the over-sampling in the data, by multiplying the number of diagonals by  $28 \text{ psec} \times 15.2 \text{ GHz}$ . 28 psec is the sampling period and 15.2 GHz is the 3 dB bandwidth of the data.

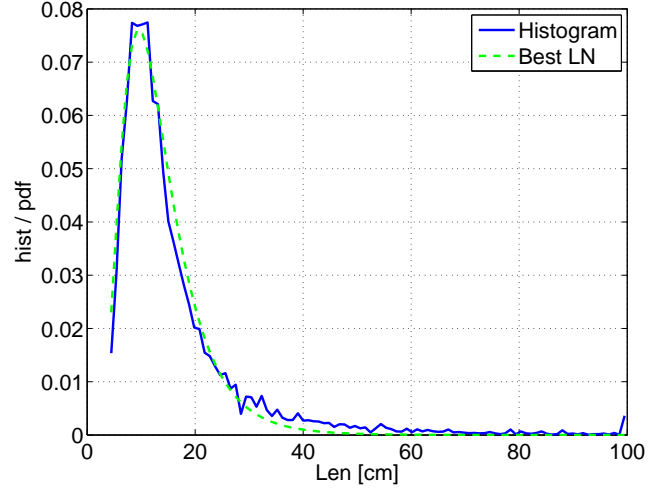


Fig. 5. A histogram of the length of extracted MPCs that account for 80% of the channel response energy, shown with the best fit log-normal distribution that has mean 13.6 cm and standard deviation 7.1 cm. The visibility length statistics (mean and standard deviation) over all extracted MPCs is are different from the statistics averaged over individual measurements.

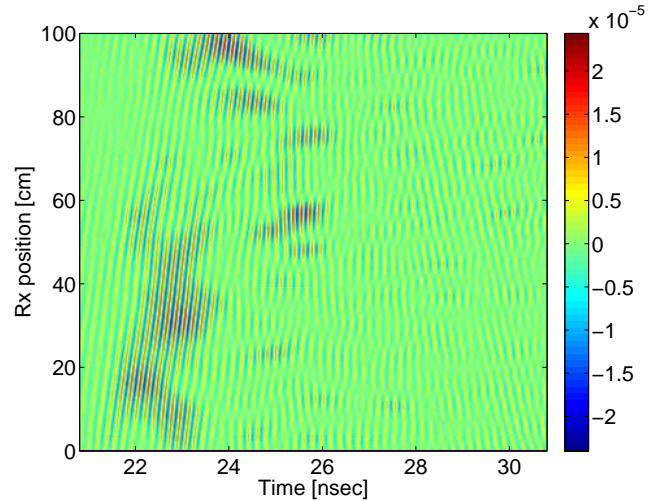


Fig. 6. An example of measured impulse responses in the 5-6 GHz band. This example is non line of sight, with terminal separation of about 6.8 meters, the terminals were located at different floors of the same building. The figure shows pass-band impulse responses measured over a one-meter rail with receiver positions separated by 2 mm. The vertical axis represents positions along the rail, the receiver was located closer to the transmitter at the top part of the picture than at its bottom. The carrier frequency (5.5 GHz in this case) was not removed in order to not lose the angle of arrival information, so the impulse response is real and shows a strong 5.5 GHz oscillation.

size of the visibility areas of the multipath components with carrier frequency increase. The reduction of both parameters is clearer in the lower bands (2-7 GHz) over the entire set of measurements; the behavior of higher bands is less consistent.

In order to appreciate the behavior of the mean diagonal length and the standard deviation against sub-band carrier frequency, we fitted them to a linear trend. Figure 8 shows one example of a linear fit of the average length of the diagonals. All of the 50 measurements show a negative slope of the average diagonal length and a negative slope of the

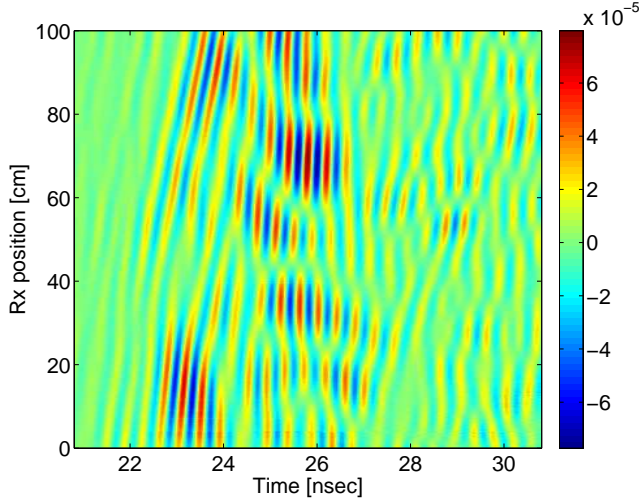


Fig. 7. An example of measured impulse responses in the 2-3 GHz band, a higher bands of the same measurement is shown in Figure 6. Note that the diagonal features (that correspond to multipath components) are *longer* in this band than in the higher band. See comments below Figure 6.

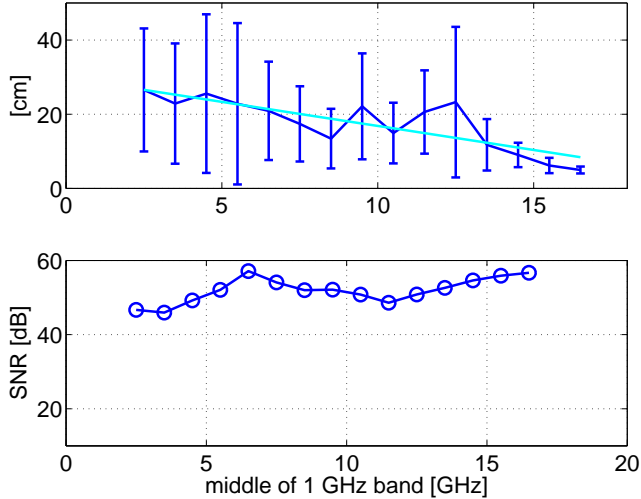


Fig. 8. The average spatial length of multipath components accounting for 80% of the measured response energy from a single typical measurement and the standard deviation, plotted in the top graph against sub-band carrier frequency. The signal to noise ratio (SNR) is indicated in the bottom graph.

standard deviation of diagonal lengths. These negative slopes indicate the reduction in the size of the visibility areas as the carrier frequency increases. More negative (steeper) slopes, that indicate a fast decrease of the size of the visibility areas, are apparent for some measurements with terminal separations below 10 meters and SNR above 40 dB.

## V. SUMMARY AND SIGNIFICANCE

This paper offers analysis of measured wideband radio channel responses, with an emphasis on the visibility of the multipath components across space.

The analysis of full-band (2-17.2 GHz) measurements extracted the significant multipath components from each measurement using a simple software tool designed for this

purpose, and compared two simplified representations of the channel to the original measurements. The simplified measurement reconstructions were performed in two ways: (1) by considering spatially limited multipath components, i.e. paths that are seen by the receiver over limited areas in space, and (2) by considering multipath components that are seen over a fixed (one meter) range of receiver positions. The second (spatially unbounded) channel representation corresponds to the accepted philosophy of channel models, i.e. the implicit assumption that multipath components are stable over a range of receiver motion. The range of receiver positions where the multipath structure is assumed to be stable is sometimes termed ‘small-scale’ without a quantitative characterization. Our results indicate that multipath components are stable over areas of space on the order of 20-30 cm. Line of sight components are more stable than non line of sight ones, in fact they are seen across the entire one-meter range of our measurements. The spatial dynamics of non line of sight radio channels appear to be dominated by the appearance and disappearance of multipath components.

The analysis of the responses with a bandwidth of 1 GHz showed that the size of the areas of visibility of the multipath components decreases as the carrier frequency is increased in the range 2 GHz – 17 GHz. We did not see a significant effect of the bandwidth on the visibility radius of multipath components.

This work is an initial step towards a spatially-dependent channel model, that will enable better design of indoor MIMO system and systems with terminal mobility. It offers a step in understanding the diffuse multipath component, a concept recently under investigation, that has been measured and characterized with lower bandwidths. *Salmi et al.* [43] propose to model diffuse scattering, also named diffuse multipath component (DMC) as a continuous distribution of channel response across delays, using a multivariate Gaussian variables with given correlation properties. The diffuse components of the response are understood in this model as essentially different from the specular components, that have a delta-like effect on the channel response. The spatio-temporal characteristics of the DMC are described in [44], the angular spread of the DMC is shown to be significantly correlated with the main arrivals. [44] indicates that distinguishing the DMC from ‘regular’ arrivals is difficult.

The physical processes causing paths to appear stable over small areas also need to be investigated, the connection between carrier frequency and the average size of the areas of visibility is especially interesting in this respect. A possible explanation follows the idea of ‘wideband Fresnel zones’ suggested in [2], [3], [4], [5], [45], defined as the area of scattering at each interaction that corresponds to the maximum carried energy from the transmitter to the receiver. Each scattering event in a path from the transmitter to the receiver is accompanied by a Fresnel zone about its center. The radius of this zone is directly related to an equivalent wavelength of the impinging wave and to the transmitter–receiver separation, and it decreases as the carrier frequency increases. The effective wavelength is estimated [4] by the mean wavelength included

in the propagating waves.

$$\lambda_c \sim (\lambda_{\min} + \lambda_{\max}) / 2 = \frac{c}{f_c - B^2/4f_c}$$

Thus, a system with a high carrier frequency experiences smaller effective scattering areas and as a result smaller areas of visibility of each multipath component.

#### ACKNOWLEDGEMENT

The authors thank Katsuyuki Haneda for his advice regarding state of the art MPC extraction methods. This work is based on measurements diligently collected by Moshe Uziel of the Hebrew University, and by Shimshon Levi, Zalman Ibragimov, Dafna Ackerman and Arik Shitrit of the Communications Laboratory of the Holon Institute of Technology. We thank them for their efforts. We thank Eli Kaminsky for the development of the first generation of the multipath extraction tool, that required much insight and effort. We also thank Prof. R. Kastner from Tel Aviv University for characterizing the antenna in his laboratory.

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