Pseudo-Random Generators

Topics

- Why do we need random numbers?
- Truly random and Pseudo-random numbers.
- Definition of pseudo-random-generator
- What do we expect from pseudorandomness?
- Testing for pseudo-randomness.
- Example for PRNG algorithm.
- Linux PRNG

Why do we need random numbers?

- Simulation
- Sampling
- Numerical analysis
- Computer programming (e.g. randomized algorithm)
- Elementary and critical element in many cryptographic protocols Usually:
 - "... Alice picks key K at random ..."
 - Cryptosystems only secure if keys random.
 - Session keys for symmetric ciphers.
 - Nonce in different protocols (to avoid replay)

Cryptography relies on randomness

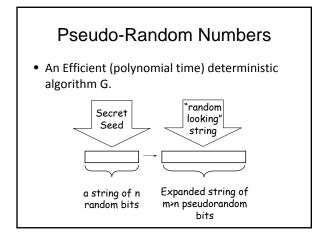
- To encrypt e-mail, digitally sign documents, or spend a few dollars of electronic cash over the internet, we need random numbers.
- If random numbers in any of these applications are insecure, then the entire application is insecure.

Truly Random Numbers

- Random bits are generated by a hardware that's based on physical phenomena.
- Those numbers cannot be reliably reproduced or predicted.
- Generation of (truly) random bits is an inefficient procedure in most practical systems: slow & expensive.
- Storage and transmission of a large number of random bits may be impractical.

Pseudo-Random Numbers

- Pseudorandom Having the appearance of randomness, but nevertheless exhibiting a specific, repeatable pattern.
- Random numbers are very difficult to generate, especially on computers which are designed to be deterministic devices.
- The sequence is not truly random in that it is completely determined by a relatively small set of initial values, called the PRNG's state.



Random looking

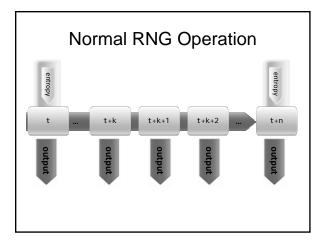
Random looking means that:

- If the number is in the range: 0...n.
- And there are m numbers to be generated.
- An observer given m-1 out of m numbers, cannot predict the mth number with better probability than 1/n.

The Seed

Can't create randomness out of nothing.

- True physical sources of randomness that cannot be predicted:
 - Noise from a semiconductor device (Hardware).
 - Resource utilization statistics and system load (Software).
 - User's mouse movements.
 - Device latencies.
- Use as a minimum security requirement the length n of the seed to a PRNG should be large enough to make brute-force search over all seeds infeasible for an attacker.



The difference between Truly Random and Pseudo-Random

If one knows: The algorithm & seed used to create the numbers.

- He can predict all the numbers returned by every call to the algorithm.
- With genuinely random numbers, knowledge of one number or a long sequence of numbers is of no use in predicting the next number to be generated.

What do we expect from pseudo-randomness?

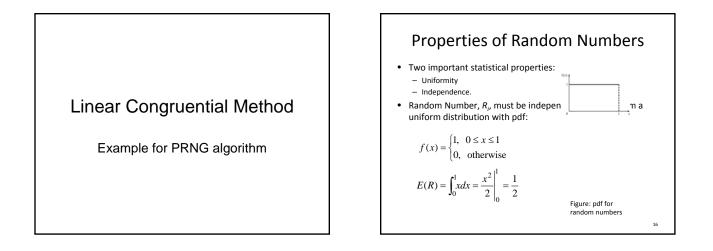
- Long period : The generator should be of long period (the period of a random number generator is the number of times we can call it before the random sequence begins to repeat).
- Fast computation: The generator should be reasonably fast and low cost.

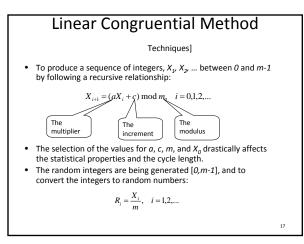
What do we expect from pseudo-randomness?

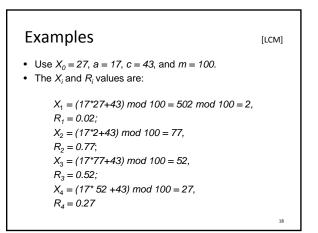
- Unbiased: The output of the generator has good statistical characteristics.
- Unpredictable: Given a few first bits, it should not be easy to predict, or compute, the rest of the bits.
- Uncorrelated sequences The sequences of random numbers should be serially uncorrelated.

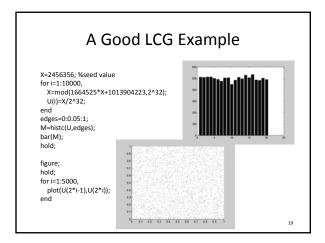
Some basic ideas for tests

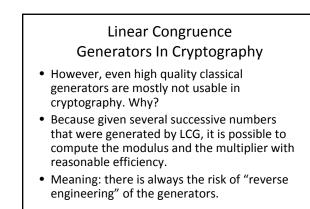
- Randomness is a probabilistic property: The properties of a random sequence can be characterized in terms of probability.
- The following tests may be applied:
 Monobit Test: Are there equally many 1's like 0's?
 - Serial Test (Two-Bit Test): Are there equally many 00, 01, 10, 11 pairs?











RNG Security Requirements

- Pseudo-randomness Output is indistinguishable from random
- Backward security RNG outputs cannot be compromised by a break-in in the past
- Forward security RNG outputs cannot be compromised by a break-in in the future

Pseudo-Random Generators In Cryptography

- If generators are needed in cryptographic applications, they are usually created using the cryptographic primitives, such as:
 - block ciphers
 - hash functions
- There is a natural tendency to assume that the security of these underlying primitives will translate to security for the PRNG.

Linux PNRG

- Implemented in the kernel.
 Entropy based PRNG
- Used by many applications - TCP, PGP, SSL, S/MIME, ...
- Two interfaces
 - Kernel interface get_random_bytes (nonblocking)
 - User interfaces /dev/random (blocking) /dev/urandom (non-blocking)

Linux PNRG

Entropy estimation

- A counter estimates the physical entropy in the LRNG
- Increased on entropy addition (from OS events)
- Decreased on data extraction.
- blocking and non-blocking interfaces
 - Blocking interface does not provide output when entropy estimation reaches zero
 Non-blocking interface always provides output
 - Blocking interface is "considered more secure"

Entropy Collection

- Events are represented by two 32-bit words - Event type.
 - E.g., mouse press, keyboard value
 - Event time in milliseconds.
- Bad news:
 - Actual entropy in every event is very limited
- Good news:
 - There are many of these events...

